

## SYLLABUS OF A MODULE

Polish name of a module	<b>Równania różniczkowe zwyczajne</b>
English name of a module	<b>Ordinary Differential Equations</b>
ISCED classification - Code	0541
ISCED classification - Field of study	<i>Mathematics</i>
Languages of instruction	<i>English</i>
Level of qualification:	<i>1</i>
Number of ECTS credit points	<i>6</i>
Examination:	<i>EW</i>
Available in semester:	<i>Y</i>

### Number of hours per semester:

Lecture	Exercises	Laboratory	Seminar	E-learning	Project
30 E	30	0	0	0	0

### **MODULE DESCRIPTION**

#### **Module objectives**

- O1. Making the students familiar with the methods to solve certain types of differential equations and systems of differential equations
- O2. Acquainting the students with theorems to existence and uniqueness of solutions of differential equations
- O3. Developing skill in formulating differential equation models which are found in applications within engineering, physics, biology and economics

### **PRELIMINARY REQUIREMENTS FOR KNOWLEDGE, SKILLS AND OTHER COMPETENCES**

1. Knowledge of linear algebra and calculus of one and several variables
2. Ability to use different sources of information
3. Ability to work both independently and in a group

4. Ability to correctly interpret and present student's own activities

### LEARNING OUTCOMES

- LO 1 – student is able to solve the selected differential equations and systems of linear differential equations and is able to give the proper interpretation of the solutions
- LO 2 – student is able to formulate and sketch the proof of the selected theorems on existence and uniqueness of solutions of differential equations
- LO 3 – student is familiar with applications of differential equations

### MODULE CONTENT

Type of classes – Lectures	Number of hours
<b>Lec 1</b> – Introduction to differential equations. Definitions and terminology. Direction fields. Modeling with differential equations.	<b>3</b>
<b>Lec 2</b> – First order differential equations: separable equations, homogeneous equations.	<b>3</b>
<b>Lec 3</b> – First order linear differential equations. Bernoulli equation.	<b>3</b>
<b>Lec 4</b> – Exact equations – definitions, method of solution. Integrating factor.	<b>3</b>
<b>Lec 5</b> – Second order differential equations. Basic concepts. Linear second order differential equations with constant coefficients.	<b>3</b>
<b>Lec 6</b> – Nonhomogeneous second order DE. Variation of parameters technique.	<b>3</b>
<b>Lec 7</b> – Method of undetermined coefficients. Second order linear differential equation with variable coefficients - Euler equation.	<b>3</b>
<b>Lec 8</b> – Systems of linear first-order differential equations. Basic theory.	<b>3</b>
<b>Lec 9</b> – Homogenous linear systems. Method of solution.	<b>3</b>
<b>Lec 10</b> – Non-homogeneous linear systems. Solutions to the nonhomogeneous systems.	<b>3</b>

<b>Type of classes – Tutorials</b>	<b>Number of hours</b>
<b>T1</b> – Classification of differential equations. Basic concepts and examples. Direction fields, isoclines, integral curves.	<b>3</b>
<b>T2</b> – Solving separable and homogeneous differential equations.	<b>3</b>
<b>T3</b> – Solving first order linear differential equations and Bernoulli equations.	<b>3</b>
<b>T4</b> – Solving exact differential equations. Integrating factor.	<b>3</b>
<b>T5</b> – Solving second order differential equations.	<b>3</b>
<b>T6</b> – Solving nonhomogeneous second order DE. Variation of parameters technique.	<b>3</b>
<b>T7</b> – Solving nonhomogeneous second order DE. Method of undetermined coefficients. Euler equation.	<b>3</b>
<b>T8</b> – Solving systems of linear first-order differential equations with real and complex eigenvalues.	<b>3</b>
<b>T9</b> – Solving nonhomogeneous systems of differential equations using undermined coefficients and variation of parameters.	<b>4</b>
<b>T10</b> – Test	<b>2</b>

### **TEACHING TOOLS**

1. – lecture with using multimedia presentations
2. – tutorials

### **WAYS OF ASSESSMENT ( F – FORMATIVE, S – SUMMATIVE**

<b>F1.</b> - assessment of preparation for exercises
<b>F2.</b> - assessment of the ability to apply the acquired knowledge while doing the exercises
<b>F3.</b> - assessment of activity during classes
<b>S1.</b> - assessment of the ability to solve the problems posed

**S2.** - assessment of mastery of the teaching material being the subject of the lecture  
- exam

\*) in order to receive a credit for the module, the student is obliged to attain a passing grade in all laboratory classes as well as in achievement tests.

## STUDENT'S WORKLOAD

L.p.	Forms of activity	Average number of hours required for realization of activity
<b>1. Contact hours with teacher</b>		
1.1	Lectures	30
1.2	Tutorials	30
1.3	Laboratory	
1.4	Seminar	
1.5	Project	
1.7	Examination	5
Total number of contact hours with teacher:		65
<b>2. Student's individual work</b>		
2.1	Preparation for tutorials and tests	40
2.2	Preparation for laboratory exercises, writing reports on laboratories	
2.3	Preparation of project	
2.4	Preparation for final lecture assessment	
2.5	Preparation for examination	20
2.6	Individual study of literature	15
Total number of hours of student's individual work:		75
Overall student's workload:		140
<b>Overall number of ECTS credits for the module</b>		6
Number of ECTS points that student receives in classes requiring teacher's supervision:		2,6
Number of <b>ECTS</b> credits acquired during practical classes including laboratory exercises and projects :		1

## **BASIC AND SUPPLEMENTARY RESOURCE MATERIALS**

1. Lecture notes
2. Zill D. G., Cullen M. R., Differential equations with boundary-value problems, Thompson Brooks/Cole 2005
3. Trench William F., Elementary differential equations with boundary – value problems, 2013
4. Polyanin A. D., Manzhirow A., V., Mathematics for engineers and scientists, Chapman & Hall/CRC, 2007

## **MODULE COORDINATOR (NAME, SURNAME, DEPARTMENT, E-MAIL ADDRESS)**

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